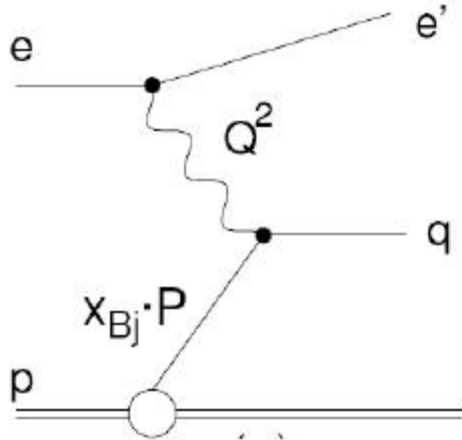


Jet Production at Low Q^2 DIS and determination of α_s

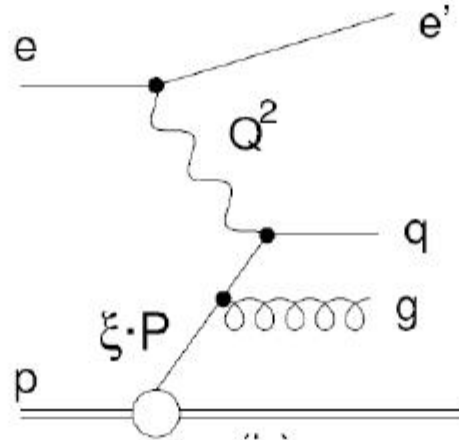
- Motivation
- Analysis:
 - Data sample, event selection
 - Correction procedure
 - Systematic errors
- Results
 - Cross sections, comparison with NLO
 - α_s fits
- Conclusions

Motivation

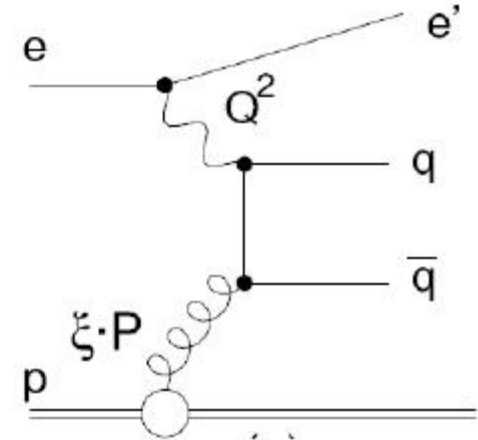
High P_T jets in Breit frame sensitive to α_s and to gluon content of the proton



Born Level



QCD Compton



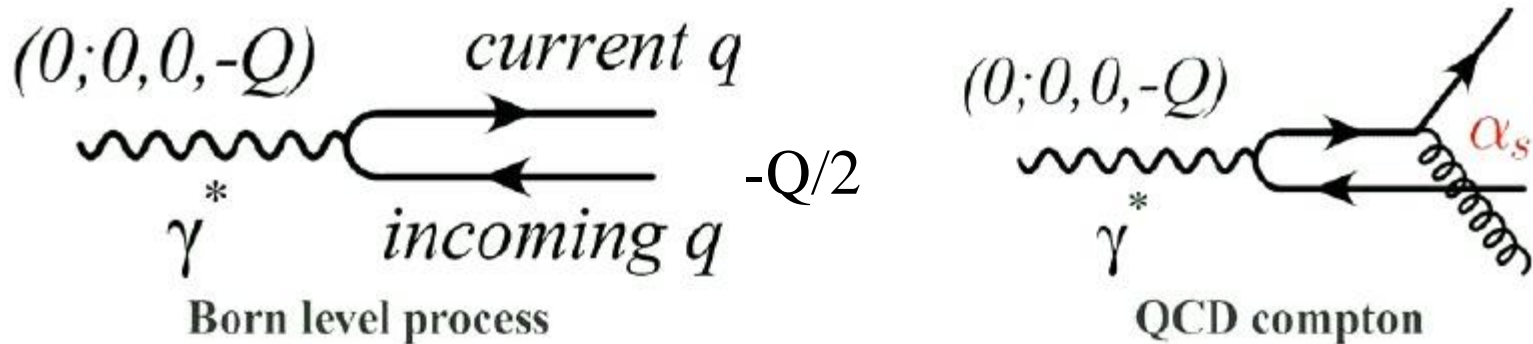
Boson Gluon Fusion

This analysis:

- Measure inclusive, 2-jets and 3-jets from HERA-1 data
- Extract α_s from these measurements

Together with high Q^2 analysis running of α_s can be tested at scales $\sim 5 \div 100$ GeV

NC Jet Production in DIS in Breit frame



Breit frame: proton and virtual photon collide head-on, in the naive quark-parton model the quark bounces off from the photon

Born level contribution is suppressed

transverse momentum in Breit frame stems mainly from QCD process

Jets well separated from the proton remnant ($P_T=0$)

longitudinally invariant k_T jet-algorithm in the Breit frame,

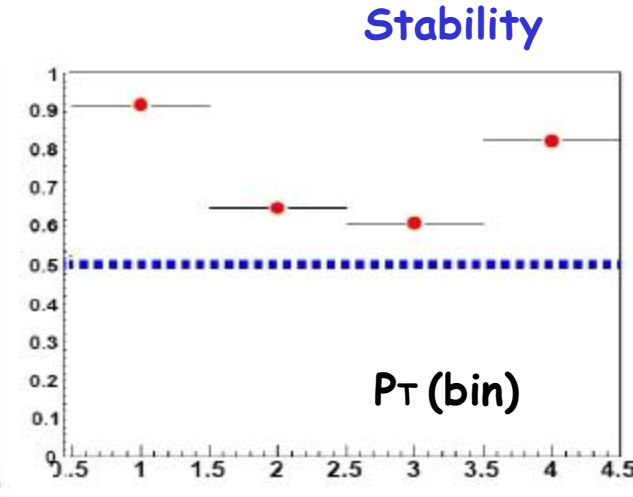
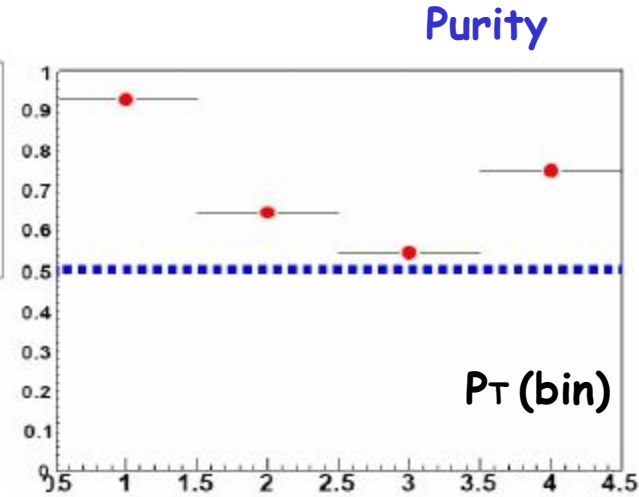
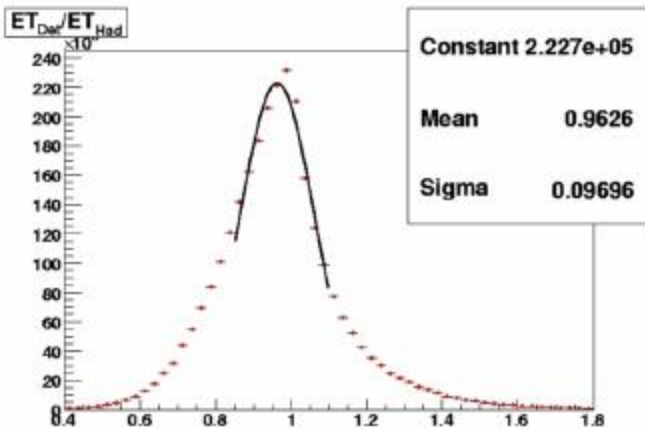
collinear and infrared safe

Low Q^2 NC DIS Jet Event Selection

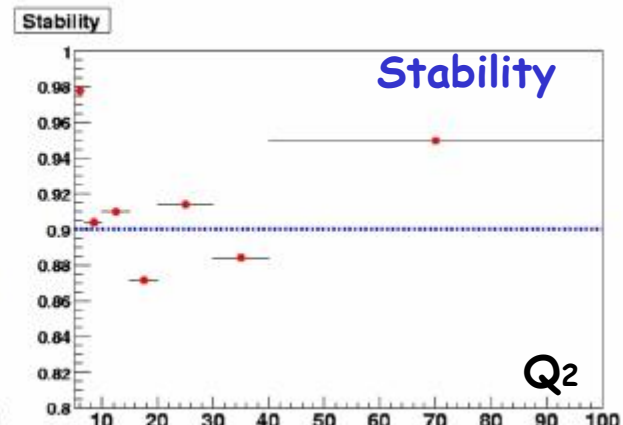
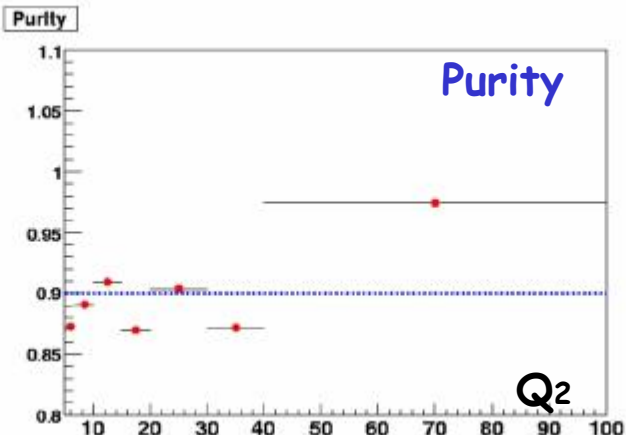
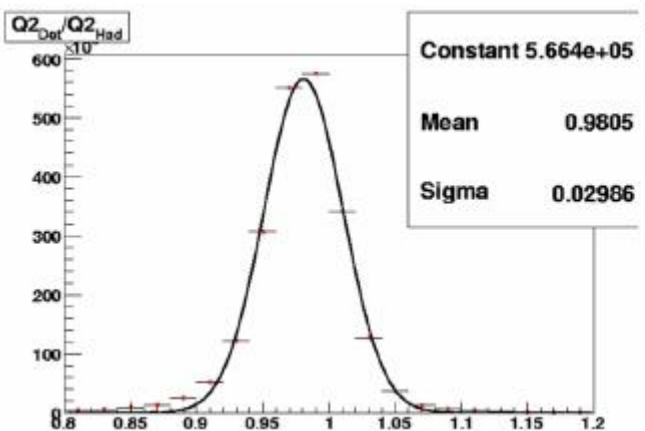
- **Kinematical Region** ($e\Sigma$ method)
 - $5 < Q^2 < 100 \text{ GeV}^2$
 - $0.2 < y < 0.7$

- **Jet Selection**
 - Inclusive kt algorithm in Breit frame
 - $P_{T\text{Breit}} > 5 \text{ GeV}$
 - $-1.0 < \eta_{\text{lab}} < 2.5$
 - for 2,3 jet cross-sections:
 $M_{j1,j2} > 18 \text{ GeV}$

Jet resolution, purity, stability vs P_T , Q_2



DJANGO



Cross-section measurements

Results are presented as differential and double differential cross-sections vs

- Q^2 , P_T for inclusive jets
- Q^2 and $\langle P_T \rangle$ for 2-jets and 3-jets, 3j/2j ratios
- Q^2 and ξ for 2-jets.

$$\langle P_T \rangle \equiv \left(\frac{P_{T,jet1} + P_{T,jet2}}{2} \right) \quad \xi \equiv x_{Bj} \left(1 + \frac{M_{jj}^2}{Q^2} \right)$$

7 bins in Q^2 (5-7-10-15-20-30-40-100 GeV^2) - for inclusive, 2-jets

4 bins in Q^2 (5-10-20-40-100 GeV^2) - for 3-jets, 3j/2j ratios

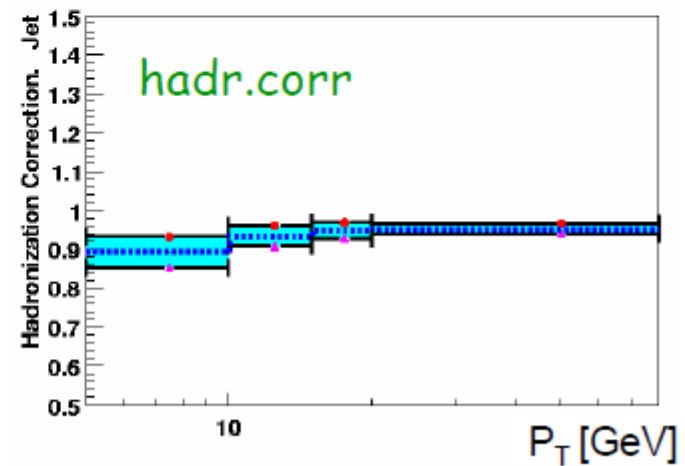
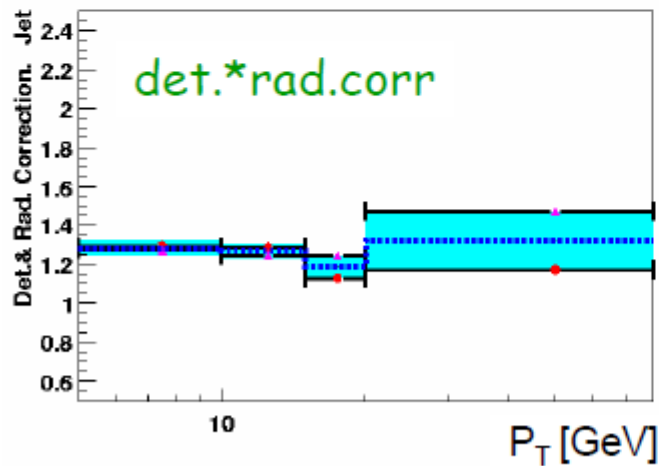
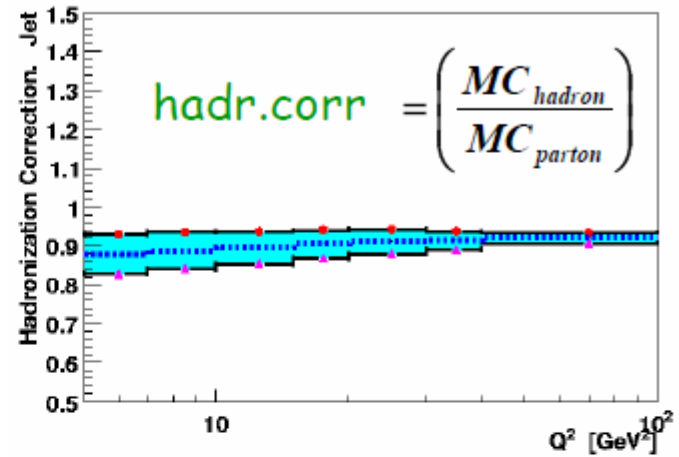
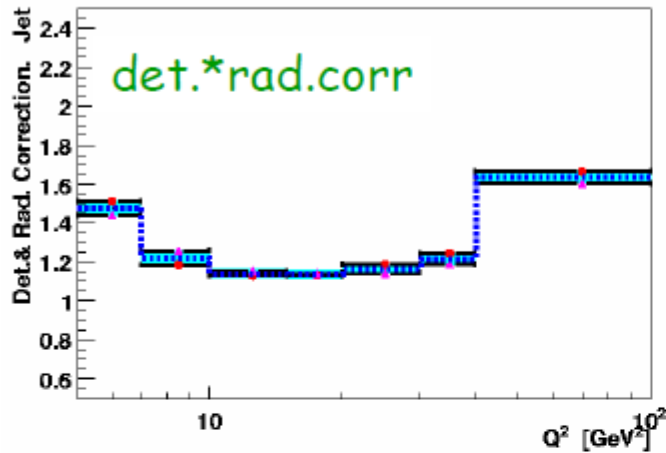
4 bins in P_T (5-10-15-20-80 GeV)

6 bins in ξ (0.004-0.006-0.01-0.025-0.05-0.1-0.3) - for 2-jets

$$\frac{d^2\sigma}{dQ^2 dP_T} = \frac{N_{events} \times \left(\frac{MC_{Hadr}^{Rad}}{MC_{Det}^{Rad}} \right) \times \left(\frac{MC_{Hadr}^{NoRad}}{MC_{Hadr}^{Rad}} \right)}{\Delta P_T \times \Delta Q^2 \times Trig.eff \times Lumi}$$

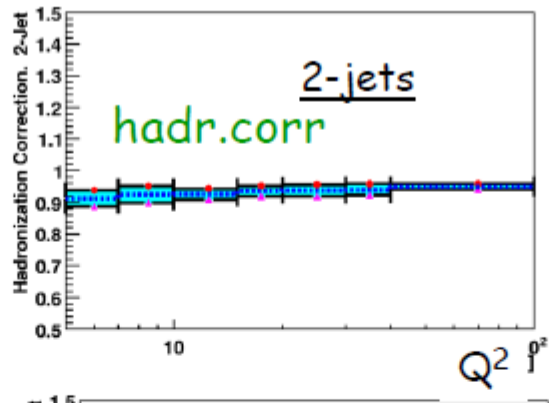
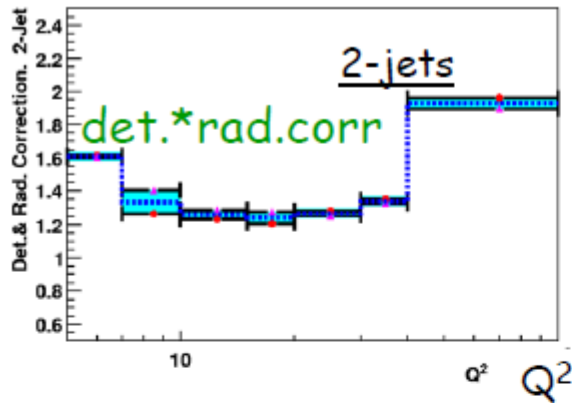
Det.Corr. Rad.Corr.

Detector×Rad and Hadronisation Corrections for incl.jets

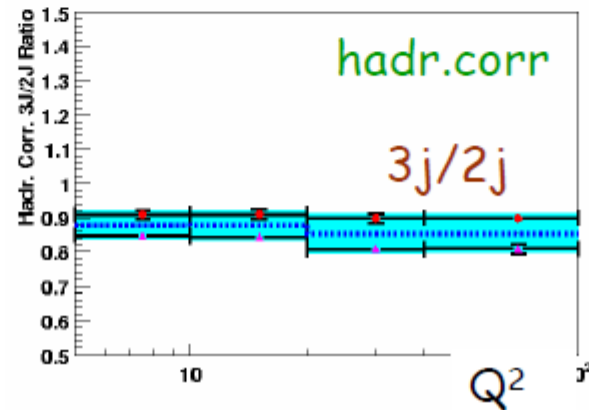
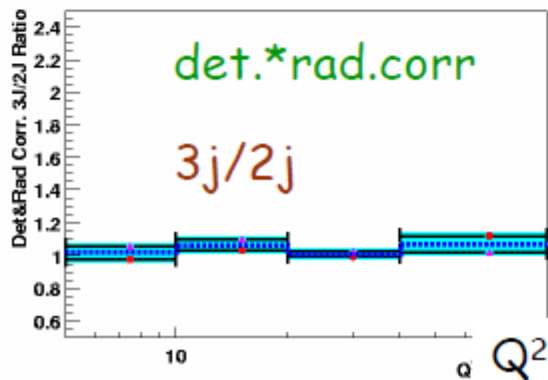
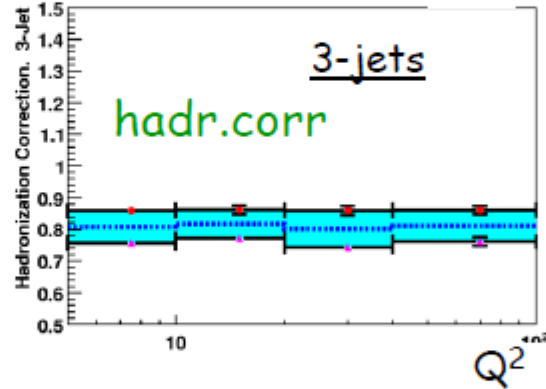
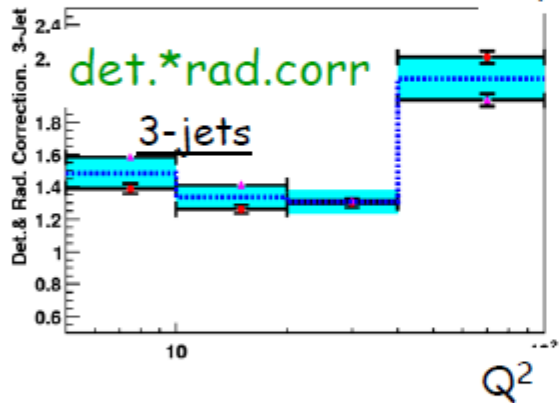


$$\text{hadr. and mod. unc.} = \left| \frac{DJANGO - RAPGAP}{2} \right|$$

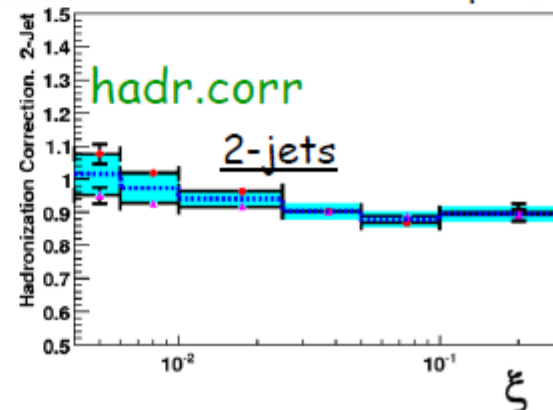
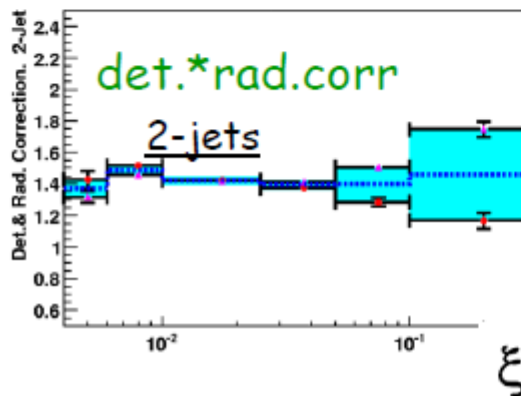
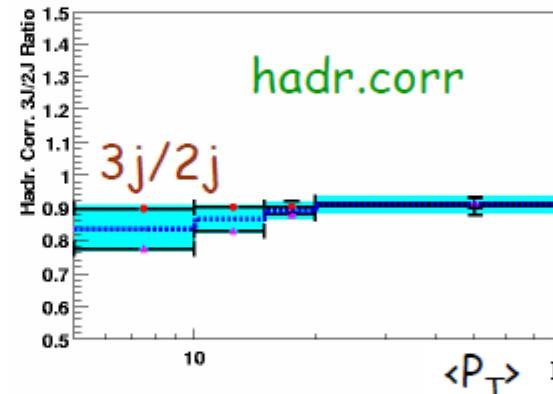
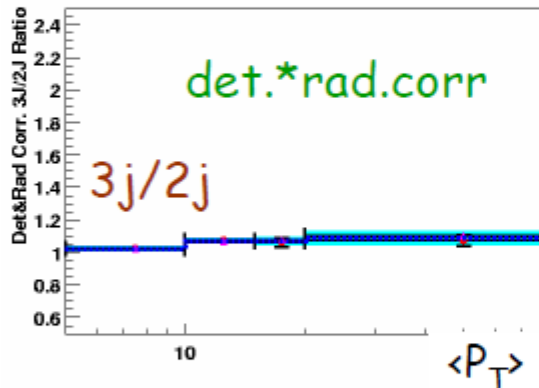
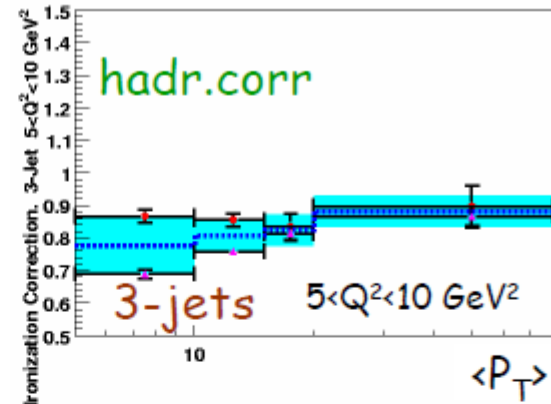
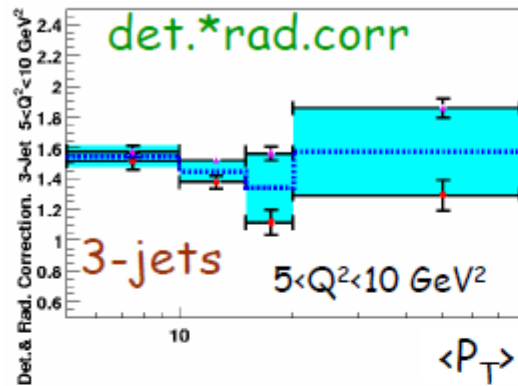
Detector x radiative, hadronisation corrections (Q^2 distributions)



$$\text{hadr. and mod. unc.} = \frac{DJANGO - RAPGAP}{2}$$



Detector x radiative, hadronisation corrections



Summary systematic errors

Systematic uncertainties are calculated for each bin

source	variation	effect on cross-section
Electron energy	$\pm 1\%$	$< 2\%$
Electron angle	$\pm 1\text{mrad}$	$< 2\%$
Hadron energy	$\pm 2\%$	$4 \div 10\%$
Model dep. (det \times rad)	(Django-Rapgap)/2	$2 \div 15\%$
lumi		1.5%
trig.eff.		$< 1\%$

Results

Cross-section measurements

- Results are presented as differential and double differential cross-sections vs
- Q^2 , P_T for inclusive jets
 - Q^2 and $\langle P_T \rangle$ for 2-jets and 3-jets, 3j/2j ratios
 - Q^2 and ξ for 2-jets.

$$\langle P_T \rangle \equiv \left(\frac{P_{T,\text{jet1}} + P_{T,\text{jet2}}}{2} \right) \quad \xi \equiv x_{Bj} \left(1 + \frac{M_{jj}^2}{Q^2} \right)$$

7 bins in Q^2 (5-7-10-15-20-30-40-100 GeV^2) - for inclusive, 2-jets

4 bins in Q^2 (5-10-20-40-100 GeV^2) - for 3-jets, 2j/3j ratios

4 bins in P_T (5-10-15-20-80 GeV)

6 bins in ξ (0.004-0.006-0.01-0.025-0.05-0.1-0.3) - for 2-jets

NLO calculation: NLOJET++

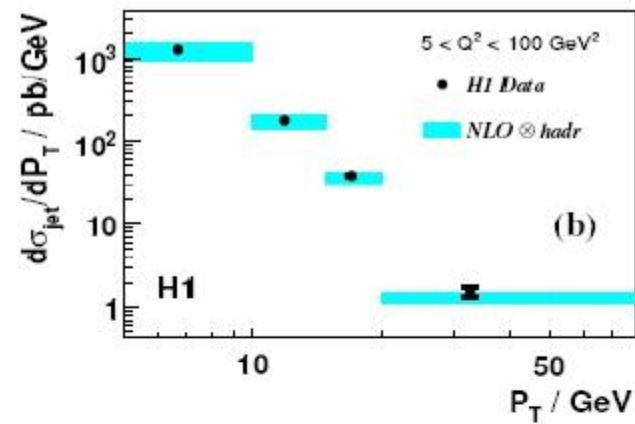
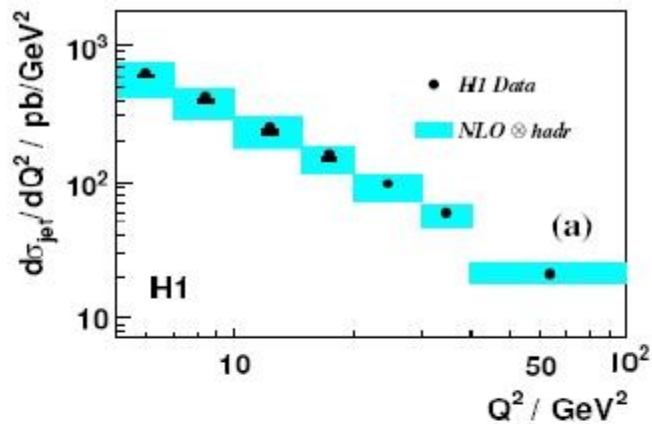
$$\mu_f, \mu_r = \sqrt{\frac{Q^2 + P_T^2}{2}}$$

$\alpha_s=0.118$

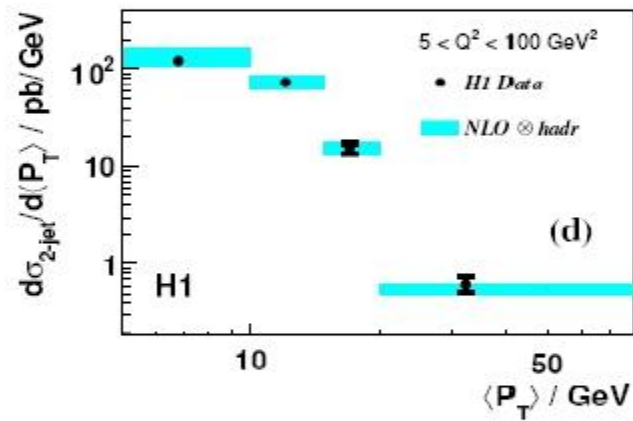
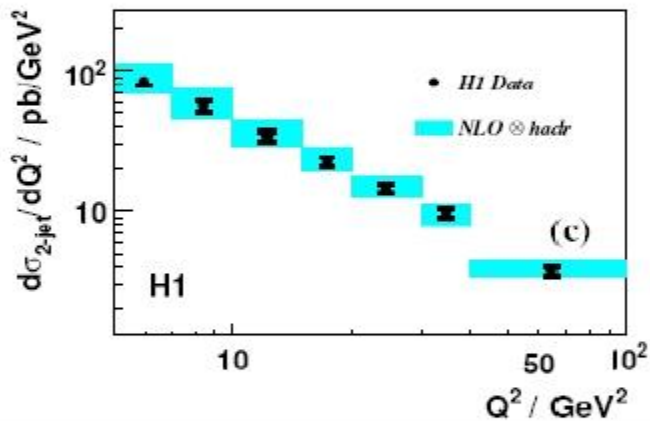
CTEQ6.5M proton PDF

Single differential cross sections vs Q^2 and P_T (or $\langle P_T \rangle$)

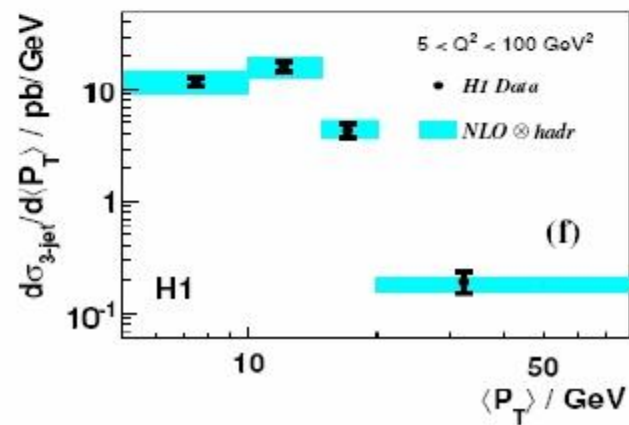
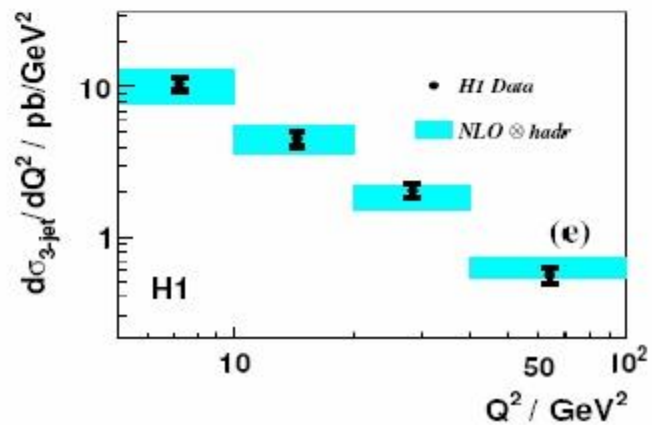
Inclusive
Jets



2-Jets

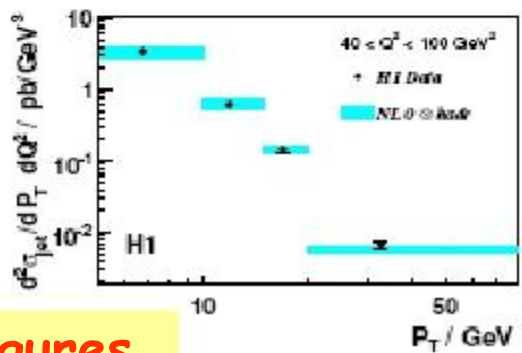
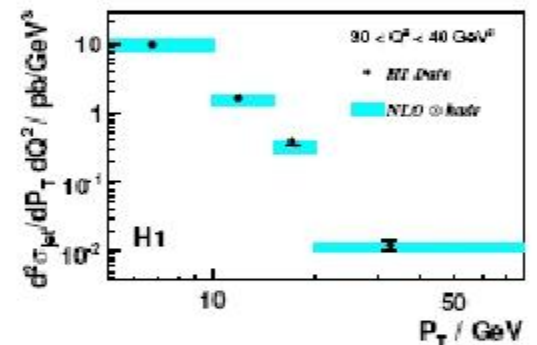
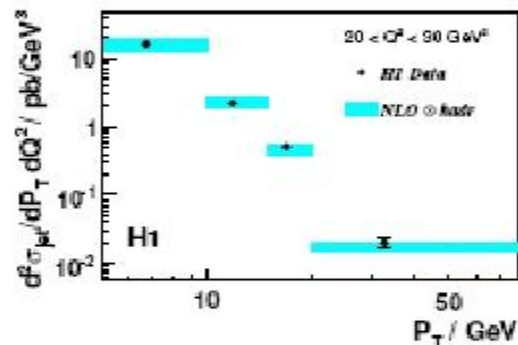
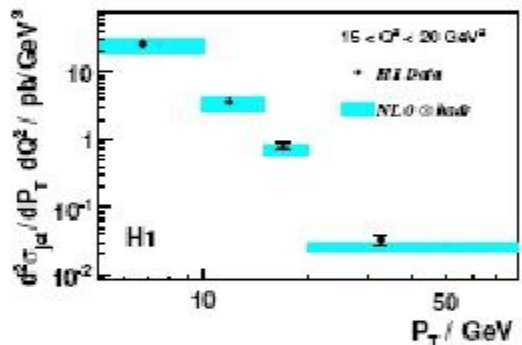
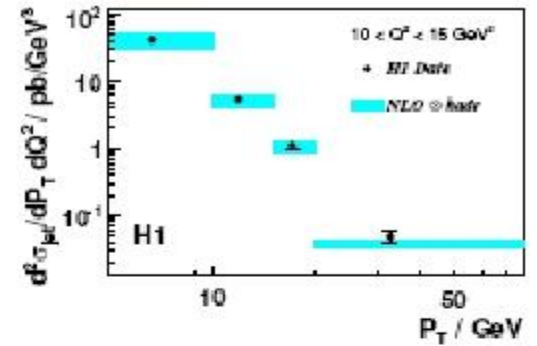
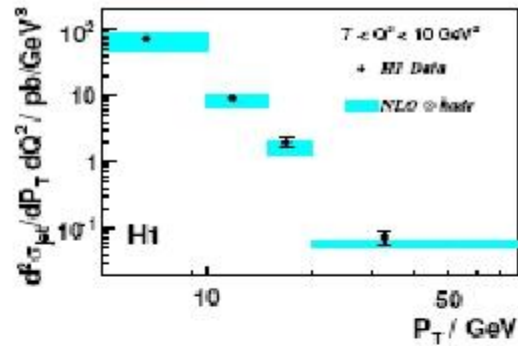
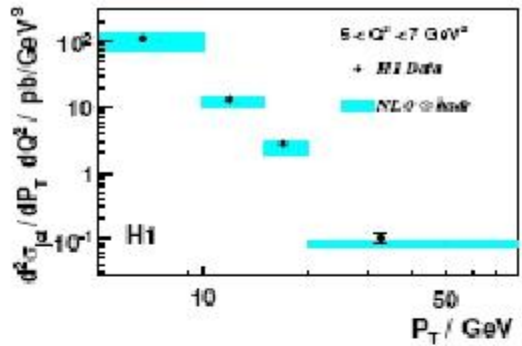


3-Jets



figures
from
paper

Double differential cross sections vs Q^2 and P_T (inclusive jets)

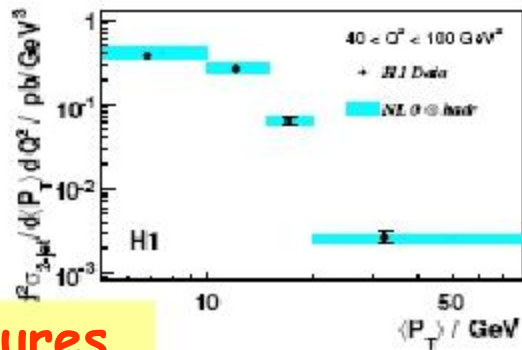
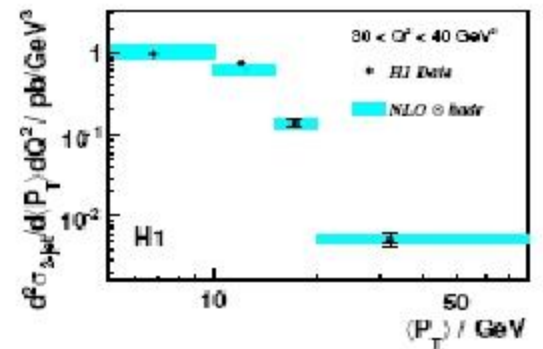
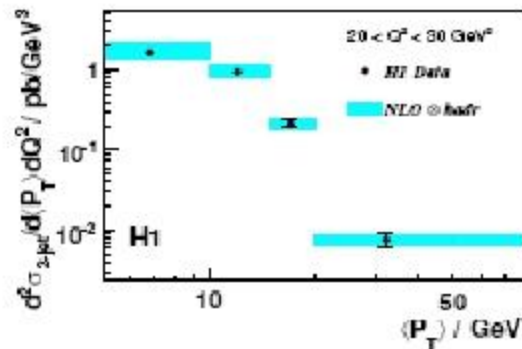
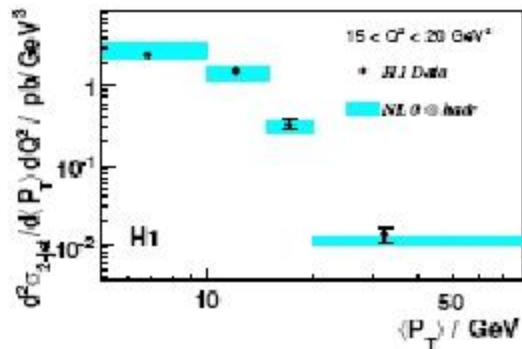
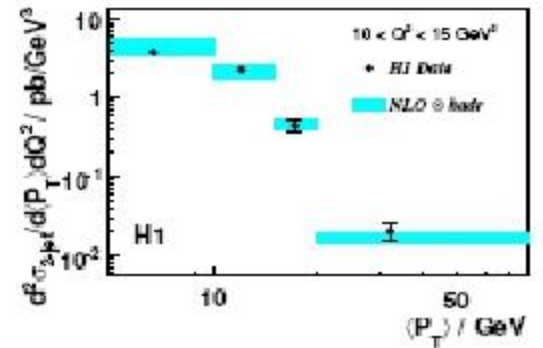
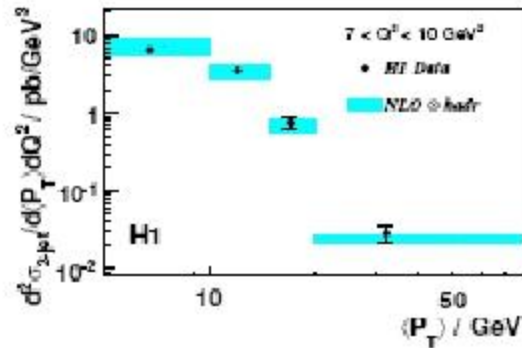
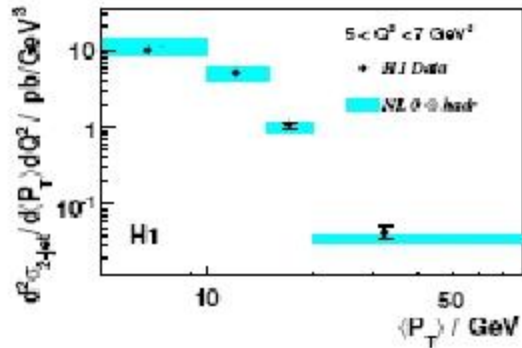


● *H1 Data*

■ *NLO \otimes hadr*

figures
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paper

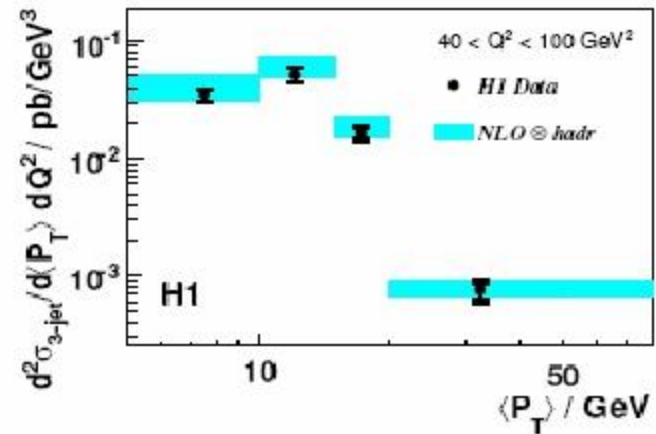
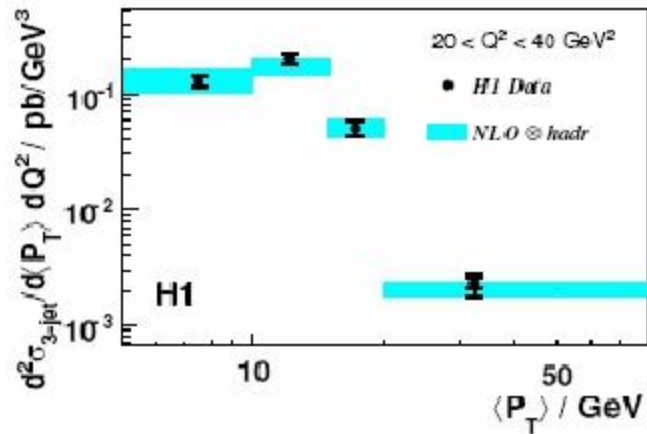
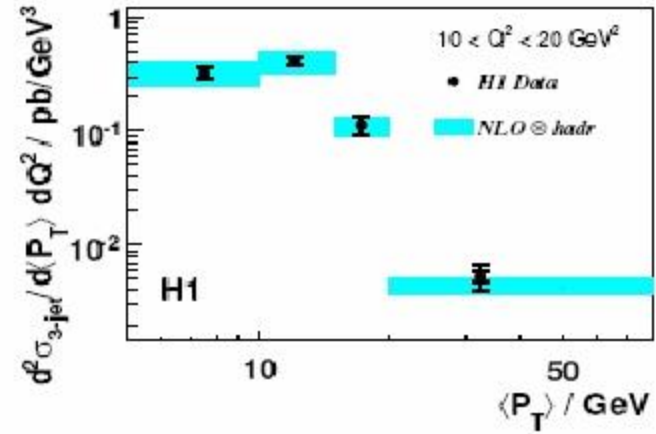
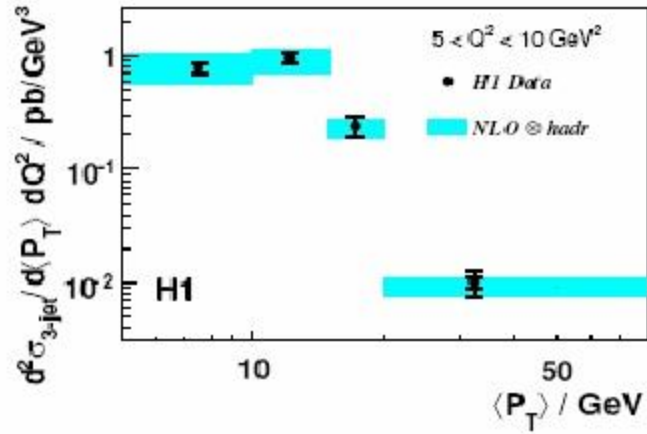
2-jets: Double differential cross sections vs Q^2 and $\langle P_T \rangle$



● *H1 Data*
 ■ *NLO \otimes hadr*

figures
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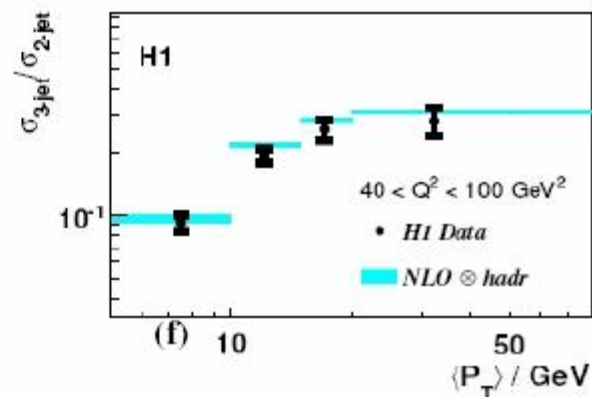
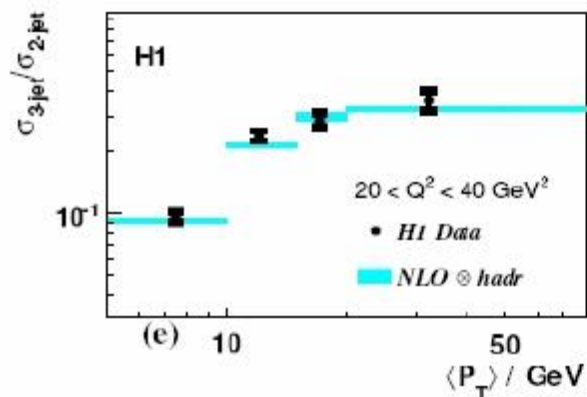
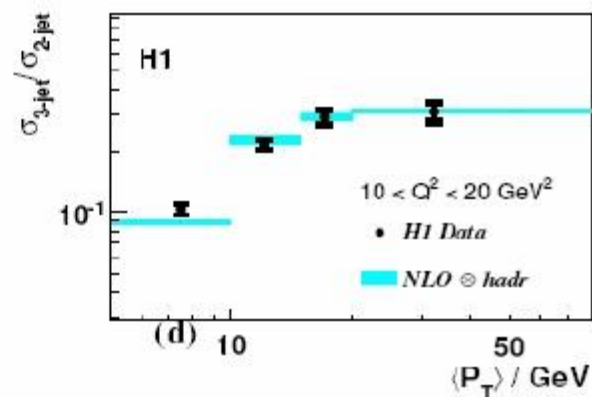
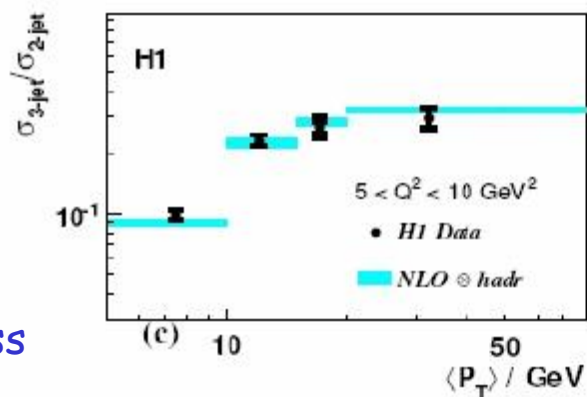
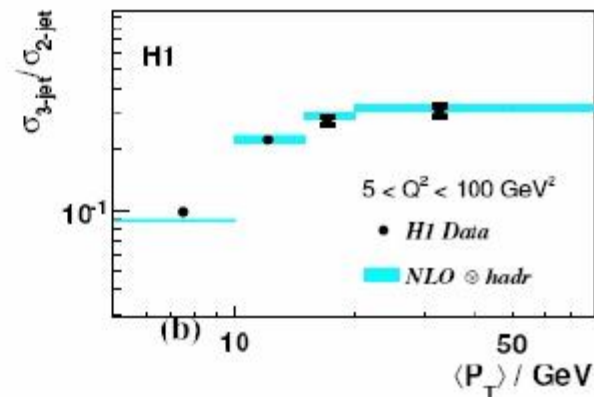
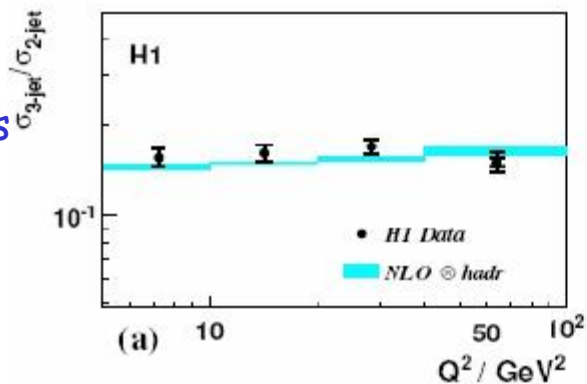
3-jets: Double differential cross sections vs Q^2 and $\langle P_T \rangle$



figures
from
paper

Ratios of $\underline{3j/2j}$ cross sections vs Q^2 and $\langle P_T \rangle$

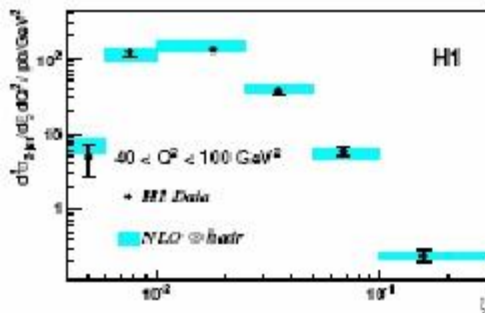
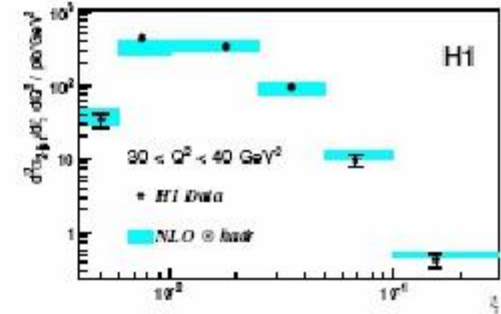
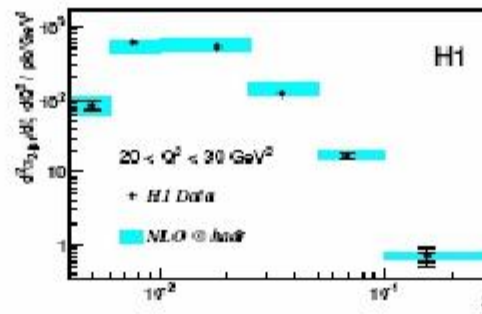
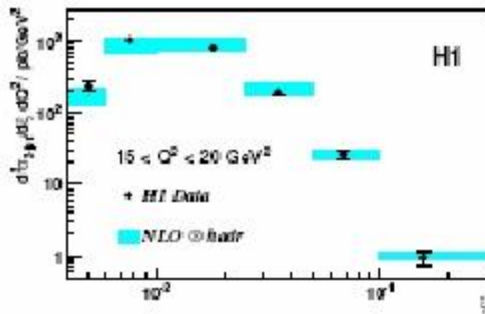
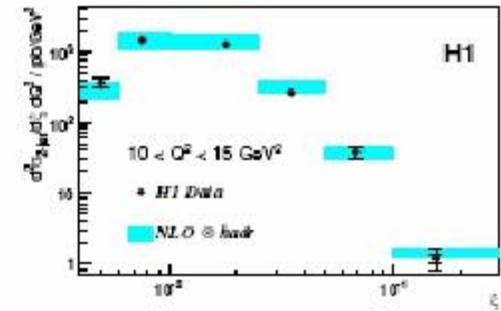
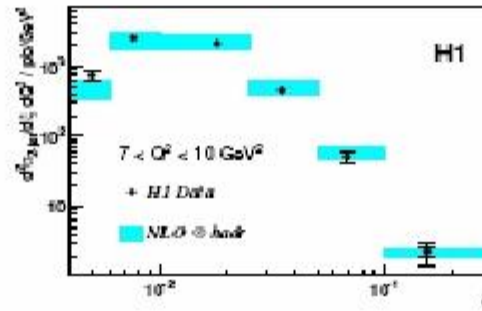
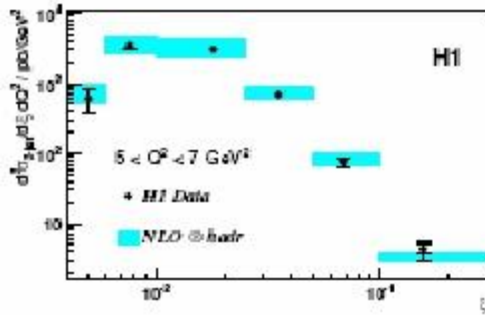
Ratios of single differential cross sections vs Q^2 and $\langle P_T \rangle$



Ratios of double differential cross sections

figures from paper

Double differential cross sections vs Q_2 and ξ (2-jets)



● *H1 Data*

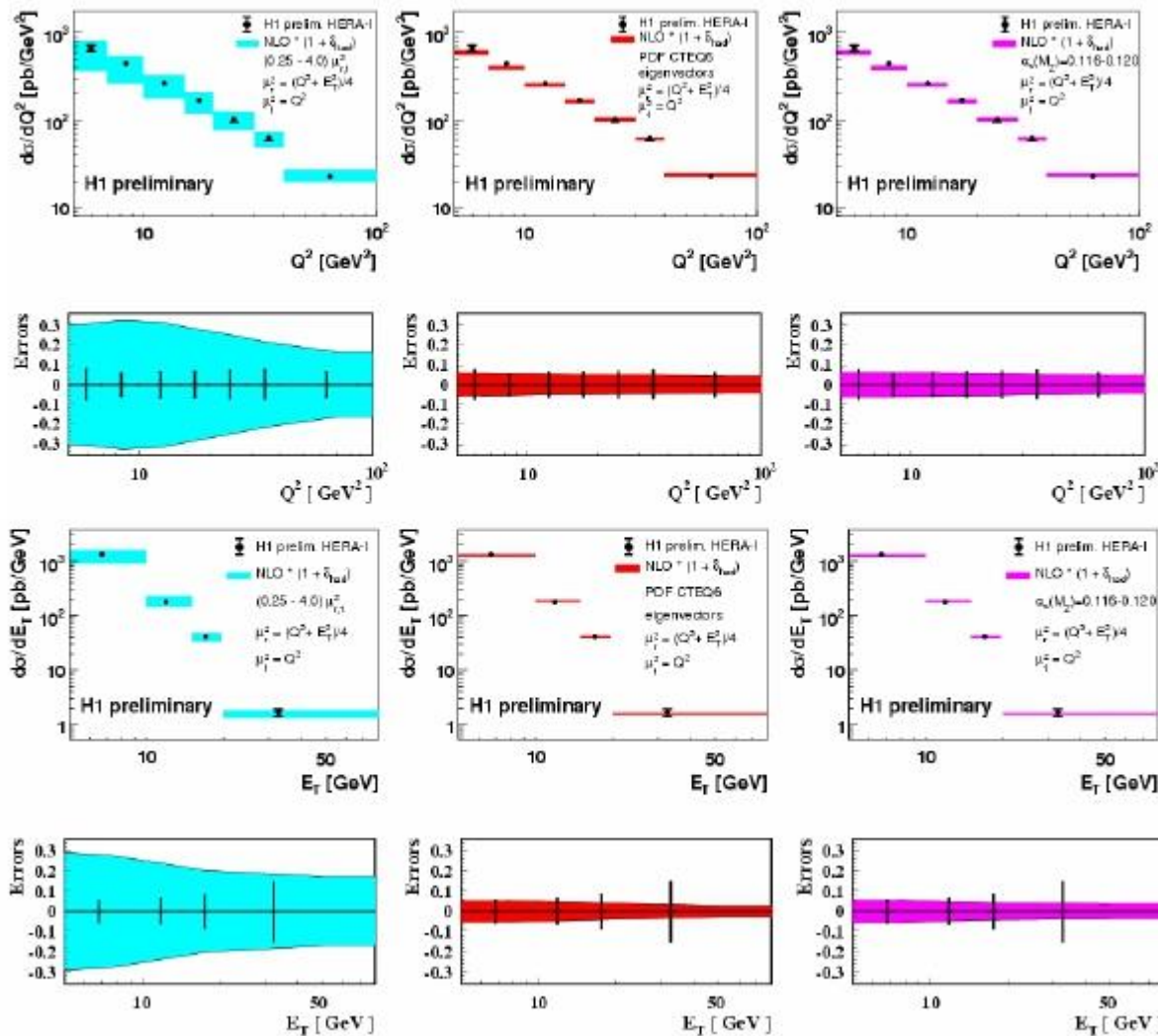
■ *NLO \otimes hadr*

As for high Q_2 paper, this distribution- $f(Q_2, \xi)$ - is introduced for PDF

Plot
from
paper

Inclusive cross-sections: compare experimental and theoretical uncertainties

Inclusive Jet Cross Sections $\frac{d\sigma}{dQ^2}$, $\frac{d\sigma}{dE_T}$



scale+hadronization

PDF

$\alpha_s(M_Z)$

Main uncertainties in NLO are from scale variation.

α_s determination

Apply same method as for high Q^2 analysis: use FASTNLO tables, Hessian method

Chi2 definition

HESSIAN χ

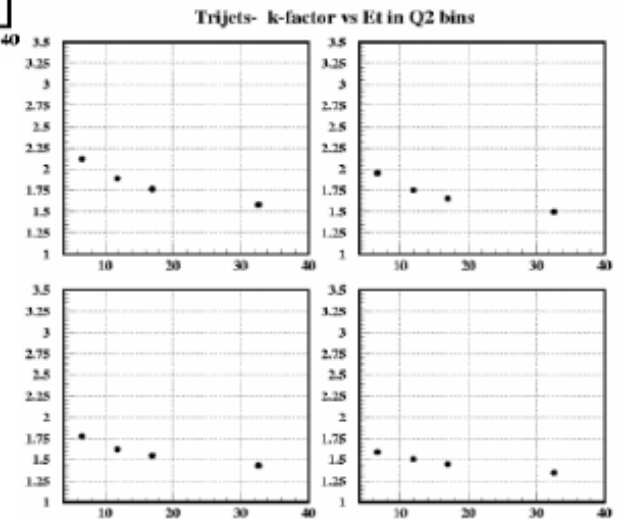
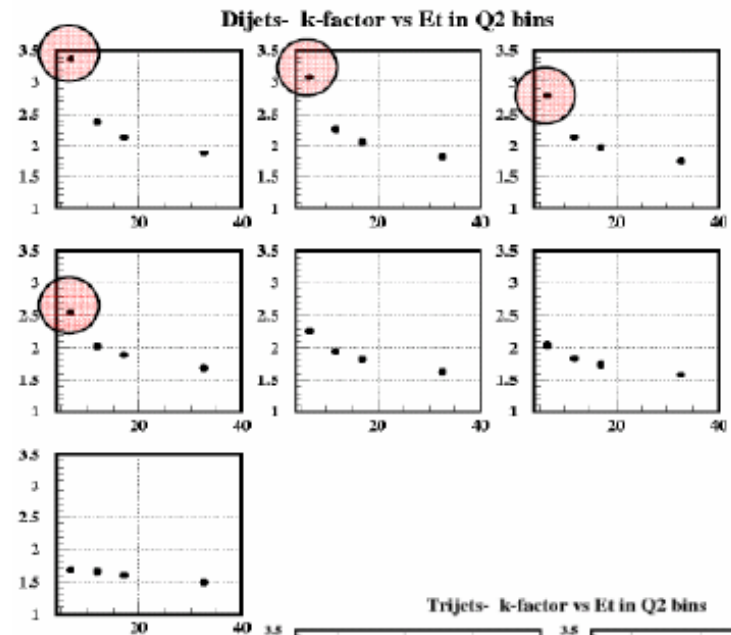
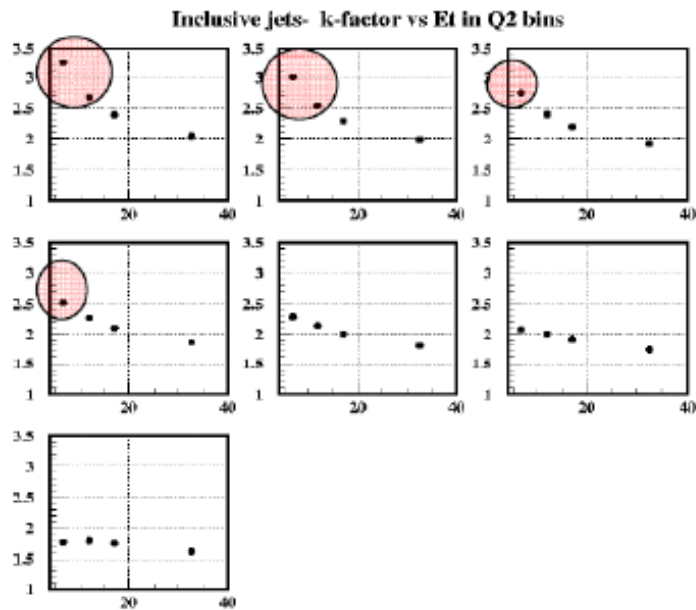
$$\chi_i = \frac{Data_i - Thr_i(1 - f_i)}{\sigma_{uncor,i}}$$

$$f_i = \sum_{\text{corr sys}} \delta_j \varepsilon_j$$

$$\chi^2 = \sum_i \chi_i^2 + \sum_{\text{corr sys}} \varepsilon_j^2$$

Cross-check with interpolation method, using NLOJET++ to calculate grids of μ_r , μ_f and α_s

k-factors (NLO/LO) vs P_T



Large k-factors (>2.5) serious doubts about convergence of perturbative series

All	K-fact.<2.5	K-fact.<2
72	62	50

Fit results comparison

Measurement	$\alpha_S(M_Z)$	α_S fit with Interpolation method
$\sigma_{\text{jet}}(Q^2, P_T)$	0.1180	0.1203
$\sigma_{2\text{-jet}}(Q^2, \langle P_T \rangle)$	0.1155	0.1155
$\sigma_{3\text{-jet}}(Q^2, \langle P_T \rangle)$	0.1170	0.1179
$\sigma_{\text{jet}}, \sigma_{2\text{-jet}}, \sigma_{3\text{-jet}}$	0.1160	0.1169

So we use FastNLO approach and extract α_s using the following data set:

1. Inclusive Jets = $f(Q^2, P_T)$ 28 bins
2. 2-jet $f(Q^2, \langle P_T \rangle)$ 28 bins
3. 3-jet $f(Q^2, \langle P_T \rangle)$ 16 bins
4. Scale choice similar to high Q^2 ($\mu_f = Q$ appear to be too small)

$$\mu_f, \mu_r = \sqrt{\frac{Q^2 + P_{T,obs}^2}{2}}$$

As FastNLO wants to operate with identical measured and scale variables ->

$P_{T,obs} = P_T$ for inclusive jet,

$P_{T,obs} = \langle P_T \rangle$ for di- and trijet.

Measurement	$\alpha_s(M_Z)$	Uncertainty			χ^2/ndf
		experimental	theory	PDF	
$\sigma_{\text{jet}}(Q^2, P_T)$	0.1180	0.0018	$+0.0122$ -0.0090	0.0022	17.5/21
$\sigma_{2\text{-jet}}(Q^2, \langle P_T \rangle)$	0.1155	0.0018	$+0.0121$ -0.0090	0.0025	14.3/23
$\sigma_{3\text{-jet}}(Q^2, \langle P_T \rangle)$	0.1170	0.0017	$+0.0090$ -0.0072	0.0014	11.0/15
$\sigma_{\text{jet}}, \sigma_{2\text{-jet}}, \sigma_{3\text{-jet}}$	0.1160	0.0014	$+0.0093$ -0.0077	0.0016	50.6/61
$\sigma_{3\text{-jet}}/\sigma_{2\text{-jet}}$	0.1215	0.0032	$+0.0066$ -0.0058	0.0013	11.9/13

for high Q^2 Jets ($Q^2 > 150 \text{ GeV}^2$) was

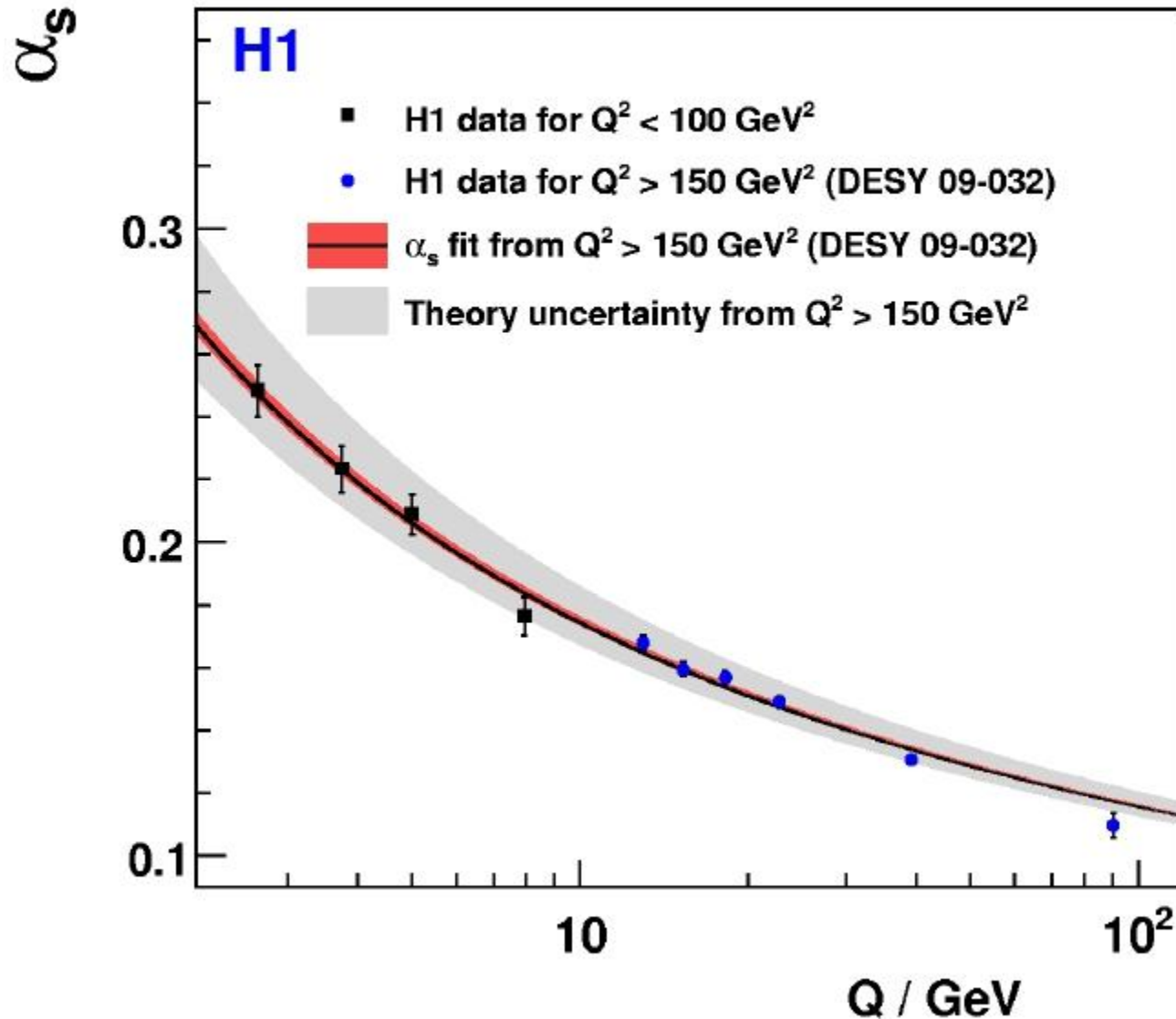
$$\alpha_s(M_Z) = 0.1168 \pm 0.0007(\text{exp.})^{+0.0046}_{-0.0030}(\text{th.}) \pm 0.0016(\text{PDF})$$

k-factor dependence

Measurement	$\alpha_S(M_Z)$	Uncertainty			χ^2/ndf
		experimental	theory	PDF	
$\sigma_{\text{jet}}, \sigma_{2\text{-jet}}, \sigma_{3\text{-jet}}$ $k\text{-factor} < 2.5$	0.1160	0.0014	+0.0093 -0.0077	0.0016	50.6/61
all k -factors	0.1171	0.0014	+0.0104 -0.0087	0.0017	95.4/71

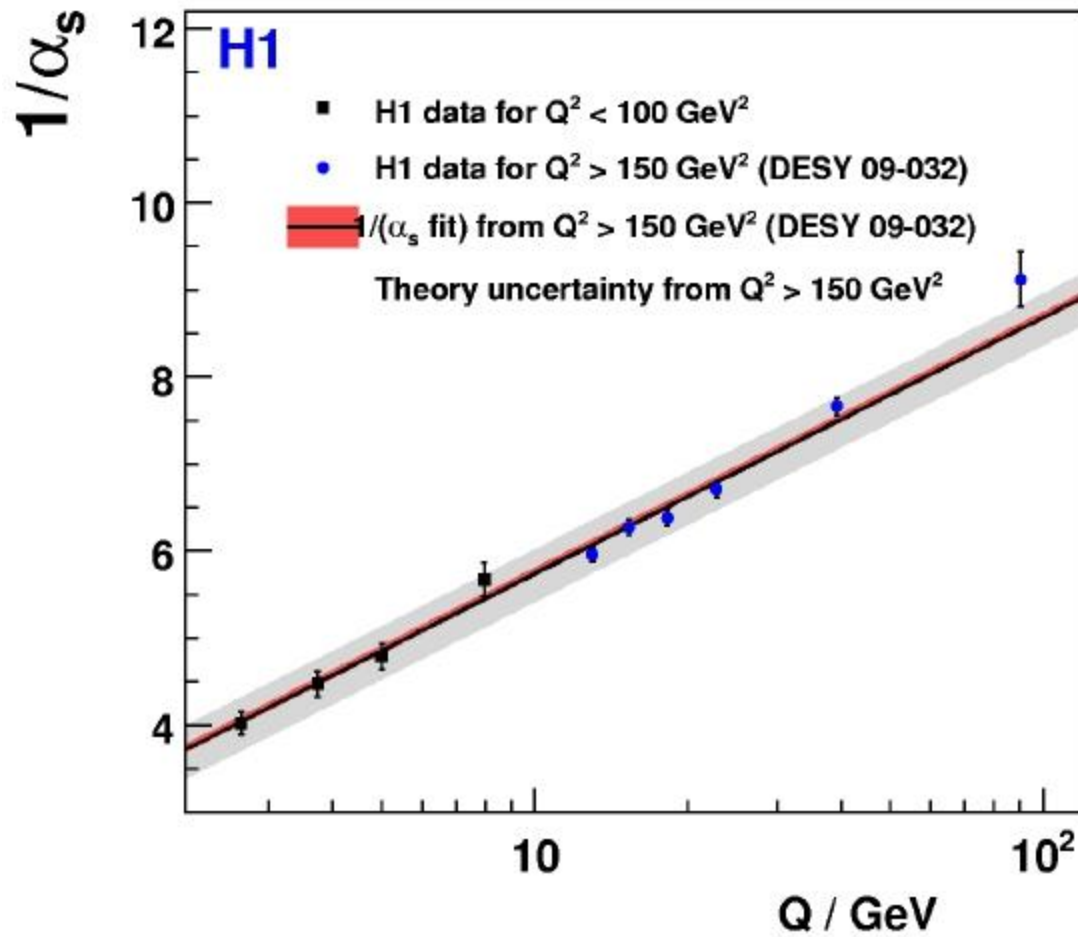
α_s Running plot

α_s from Jet Cross Sections

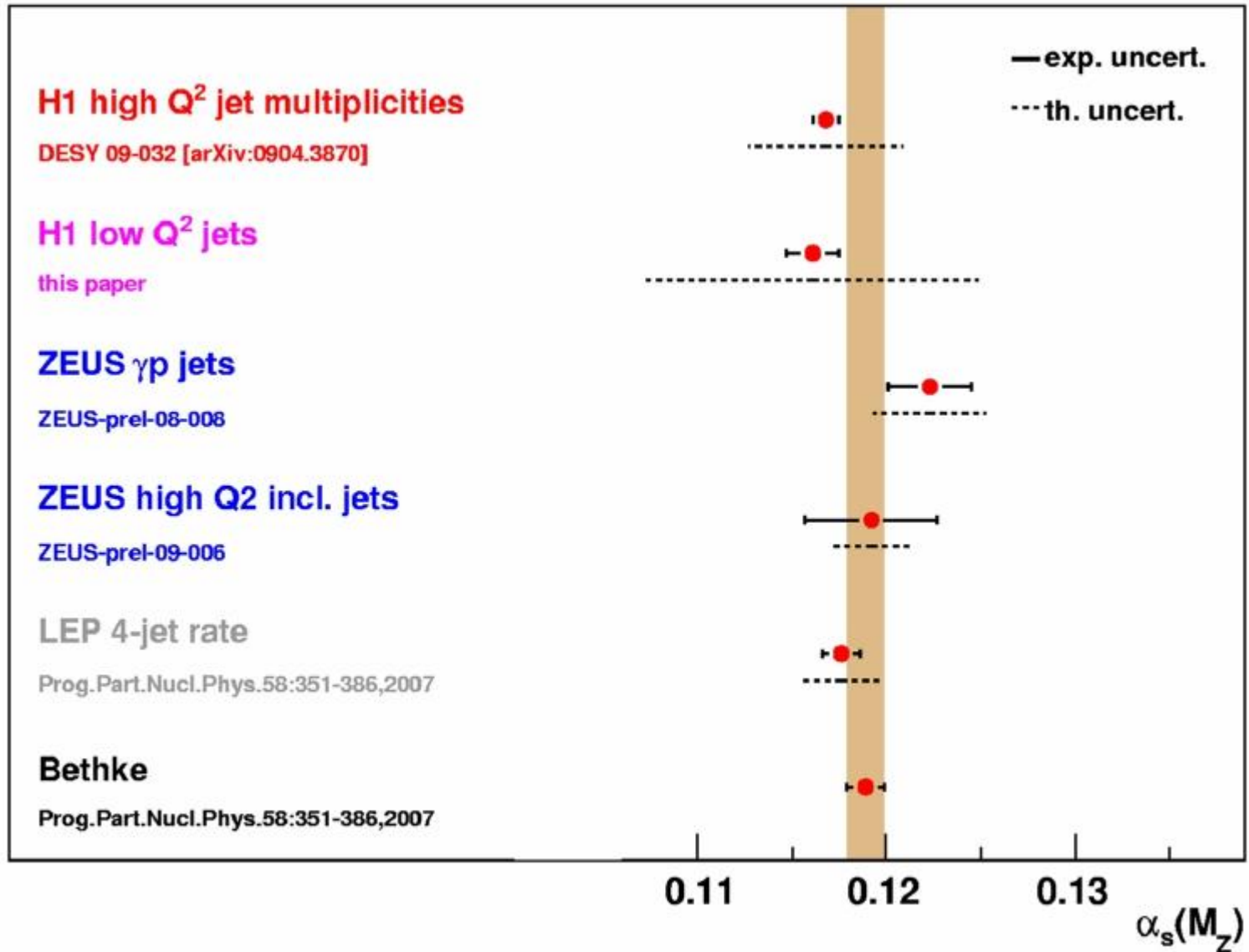


figures
from
paper

α_s from Jet Cross Sections



α_s summary



Summary

- The first time in the world differential and double differential cross sections for inclusive, di-jet and three-jet cross sections at low Q^2 DIS are measured (Eur.Phys.J. C67 (2010) 1, 11/09)
- the measured cross sections are in good agreement with NLO QCD calculations (NLOJET++) using the renormalization scale $\mu_{r2} = (Q^2 + P_{T2})/2$
 - NLO scale uncertainty is the dominant theory uncertainty
- α_s is determined from the fit to the data. It is consistent between different points and is in good agreement with the measurements at high Q^2